Can you write a C# program that creates a list of employees, where each employee has properties such as Id, Name, Age, and Department? The program should:

1. Allow adding employees to the list.
2. Display the list of all employees.
3. Include an option to filter employees by department.